Negation of statement A: a statement B whose assertion specifically denies the truth of statement A.

- 1. Negate the below statements and express the negations in English avoiding the use of negation words whenever possible.
  - (a) There is a vaccine in the world that is not safe for lizard.
  - (b) All pairs of students who participated in Geometry Mela stood atleast 6 feet apart.
  - (c) In Breakout room 2 of online class in SWMS all students were silent.
  - (d) During the month of May Siva, Sanitized his hands every hour.
  - (e) There is one person in Immunity's birthday party who is not wearing a mask.
  - (f) Every student in this class has taken Tulu or Kokborok in Class XII.
  - (g) Every student in this class has taken Mathematics and Biology in Class XII.
  - (h) In every batch of SWMS there is a student who has taken neither Mathematics nor Biology in high school.

## 2. Let us introduce Logical Notation:

- $\forall$  to mean for all;
- $\exists$  to mean there exists;
- $\implies$  to mean implies; and
- $\iff$  to mean equivalent.

Here is an example of usage of notation:

Statement : For all  $\epsilon > 0$  there is an N such that for all  $n \ge N$ ,  $a_n \in (a - \epsilon, a + \epsilon)$ . Statement in logical Notation:  $\forall \epsilon > 0$ ,  $\exists N$  such that  $\forall n \ge N$ ,  $a_n \in (a - \epsilon, a + \epsilon)$ .

(a) We say  $\lim_{n\to\infty} a_n = 3$  if

For every  $\epsilon > 0$  there exists N > 0 such that  $|a_n - 3| < \epsilon$  whenever  $n \ge N$ .

- i. Provide three examples of sequences that converge to 3.
- ii. Provide three examples of sequences that do not converge to 3.
- iii. Provide an example of sequence that does not converges to any real number.
- iv. Write a logical statement that is equivalent to saying  $\lim_{n\to\infty} a_n \neq 3$
- v. Write a logical statement that is equivalent to saying that the sequence  $a_n$  does not converge to any real number.