1. Suppose we are given $f:[a,b] \to \mathbb{R}$ and the values of $(a, f(a)), (\frac{a+b}{2}, f(\frac{a+b}{2})), (b, f(b)).$

(a) Find the line $p_1: [a,b] \to \mathbb{R}$ passing through (a,f(a)) and (b,f(b))

(b) Find the quadratic $p_2: [a,b] \to \mathbb{R}$ passing through $(a, f(a)), (\frac{a+b}{2}, f(\frac{a+b}{2})), (b, f(b))$

(c) Fill in the following table:

c

| Approximation of $\int_a^b f(x) dx$ | |
|---|--|
| $(\text{Linear})\int_{a}^{b}p_{1}(x)dx$ | |
| (Quadratic) $\int_{a}^{b} p_{2}(x) dx$ | |