$\qquad$

1. Suppose we are given $f:[a, b] \rightarrow \mathbb{R}$ and the values of $(a, f(a)),\left(\frac{a+b}{2}, f\left(\frac{a+b}{2}\right)\right),(b, f(b))$.
(a) Find the line $p_{1}:[a, b] \rightarrow \mathbb{R}$ passing through $(a, f(a))$ and $(b, f(b))$
(b) Find the quadratic $p_{2}:[a, b] \rightarrow \mathbb{R}$ passing through $(a, f(a)),\left(\frac{a+b}{2}, f\left(\frac{a+b}{2}\right)\right),(b, f(b))$
(c) Fill in the following table:

| Approximation of $\int_{a}^{b} f(x) d x$ |  |
| :---: | :---: |
| (Linear) $\int_{a}^{b} p_{1}(x) d x$ |  |
| (Quadratic) $\int_{a}^{b} p_{2}(x) d x$ |  |

